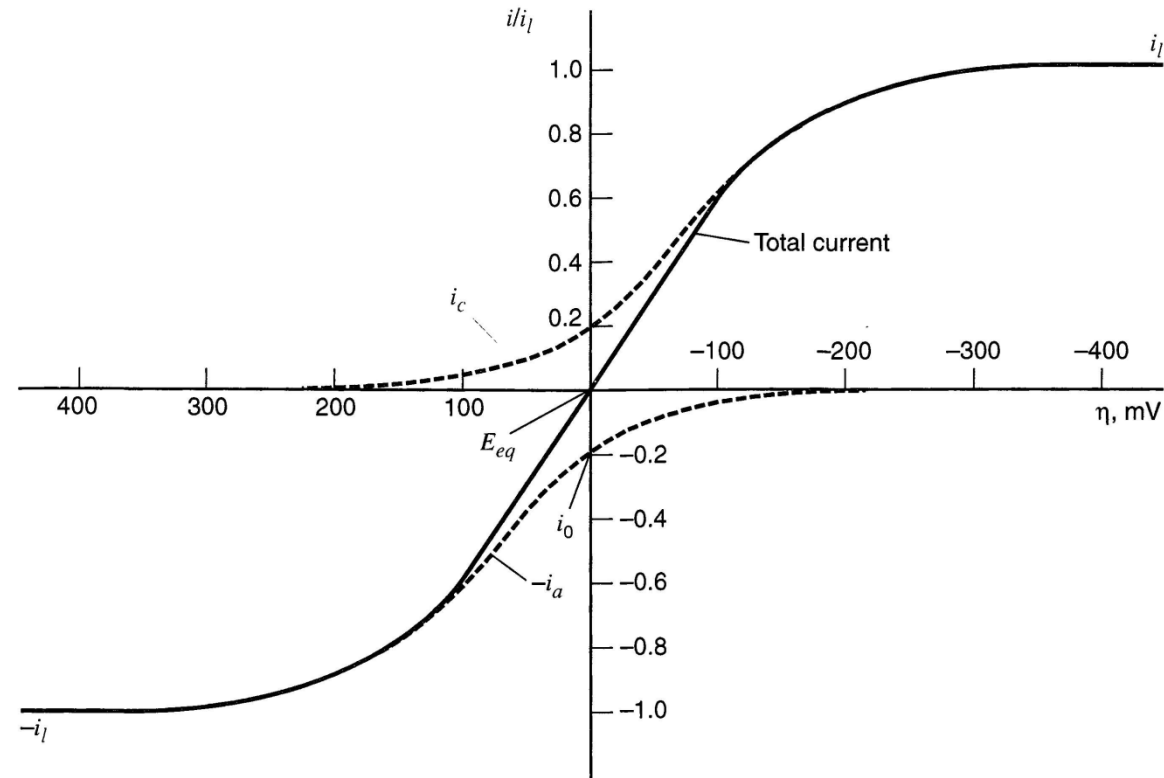


Derivation of Tafel Equation

For a reversible reaction on surface: $Ox + e \leftrightarrow Red$ E^0



$$i = F A k^0 \left[C_{O(0, t)} e^{-\alpha f (E - E^0)} - C_{R(0, t)} e^{(1-\alpha) f (E - E^0)} \right]$$

$f = F/RT$, C_O , C_R = concentration
 α = transfer coefficient

When $|\eta| \geq 100$ mV, the back-reaction is insignificant and can be neglected

$$i = 0, \text{ when } FAk^0C_O(0, t)e^{-\alpha f(E_{eq}-E^{0'})} = FAk^0C_R(0, t)e^{(1-\alpha)f(E_{eq}-E^{0'})} = i_o$$

i_o = exchange current

Assuming the surface concentration is close to bulk concentration

$$i = i_o \left[e^{-\alpha f \eta} - e^{(1-\alpha)f \eta} \right]$$

When the absolute value of $\eta \geq 100$ mV, then the back reaction is negligible, we have

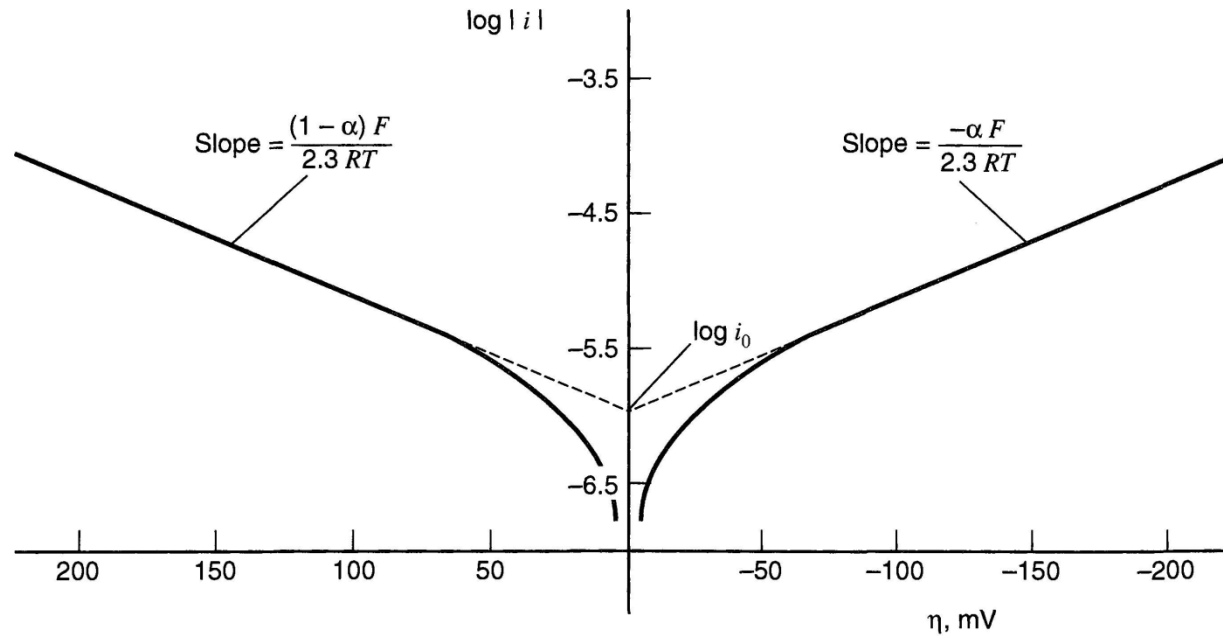
$$i = i_o \exp(-\alpha F \eta / RT) \quad \text{or} \quad \eta = \frac{RT}{\alpha F} \ln i_o - \frac{RT}{\alpha F} \ln i$$

This is the deduction of Tafel equation: $\eta = a + b \log i$

$b = -(2.3RT/\alpha F)$, when $\alpha = 0.5$, $b = 118$ at r.t. b is called Tafel slope

Both exchange current and Tafel slope are obtained from the plot of η vs. $\log i$

Plot of $\log i$ and overpotential can give i_0 and Tafel slope



In electrochemistry, we use current density to describe the reaction rate $J = i/A$, i is the current, and A is the surface area.